

# Introduction to dynamic semantics

## Session 2: Compositional discourse representation theory

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28 Jun 2024



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1 Recap

2 Problem

3 Compositional DRT

4 Practice

# Recap

The “meaning” of a sentence is its potential to change the context.

$w$	$w$	$w$	$w$
$w$	$w$	$w$	$w$
$w$	$w$	$w$	$w$
$w$	$w$	$w$	$w$

# Recap

The “meaning” of a sentence is its potential to change the context.



Evelyn  
marries  
Waymond.

# Recap

The “meaning” of a sentence is its potential to change the context.

Evelyn  
owns a  
laundromat.



Evelyn  
marries  
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# Recap



Sentences introduce **discourse referents** and **conditions** on these drefs.



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(2) Evelyn owns a laundromat.

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Sentences introduce **discourse referents** and **conditions** on these drefs.

(1) Evelyn marries Waymond.

1
Evelyn marries 2

2
Waymond marries 1

(2) Evelyn owns a laundromat.

1
Evelyn marries 2 owns 3

2
Waymond marries 1

3
is a laundromat

## Recap

The contribution of a sentence can be represented as a **discourse representation structure (DRS)**.

A DRS combines multiple cards into one.

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$u_1$ $u_2$
Evelyn( $u_1$ ) Waymond( $u_2$ ) Marry( $u_1, u_2$ )

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(3) Evelyn marries Waymond.

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(4) Evelyn owns a laundromat.

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The contribution of a sentence can be represented as a **discourse representation structure (DRS)**.

A DRS combines multiple cards into one.

(3) Evelyn marries Waymond.

$u_1$ $u_2$
Evelyn( $u_1$ ) Waymond( $u_2$ ) Marry( $u_1, u_2$ )

(4) Evelyn owns a laundromat.

$u_3$
Laundromat( $u_3$ ) Own( $u_1, u_3$ )

DRSs can be combined using **dynamic conjunction** (;).

(5) Evelyn marries Waymond. Evelyn owns a laundromat.

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(5) **Evelyn marries Waymond.** Evelyn owns a laundromat.

$u_1$ $u_2$
Evelyn( $u_1$ ) Waymond( $u_2$ ) Marry( $u_1, u_2$ )

DRSs can be combined using **dynamic conjunction** (;).

(5) Evelyn marries Waymond. Evelyn owns a laundromat.

$u_1$ $u_2$	$u_3$
Evelyn( $u_1$ ) Waymond( $u_2$ ) Marry( $u_1, u_2$ )	Laundromat( $u_3$ ) Own( $u_1, u_3$ )

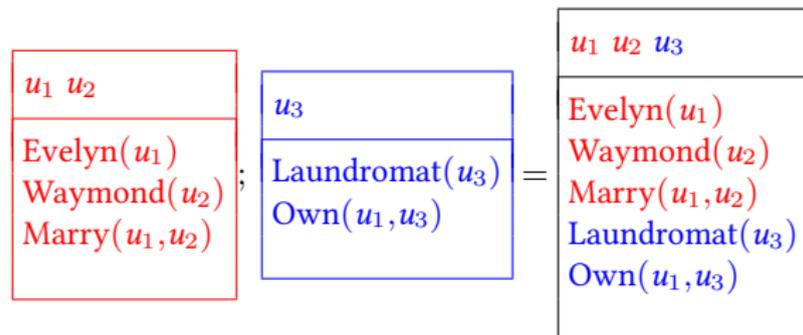
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(5) Evelyn marries Waymond. Evelyn owns a laundromat.

$u_1$ $u_2$	
Evelyn( $u_1$ ) Waymond( $u_2$ ) Marry( $u_1, u_2$ )	;
	$u_3$
	Laundromat( $u_3$ ) Own( $u_1, u_3$ )

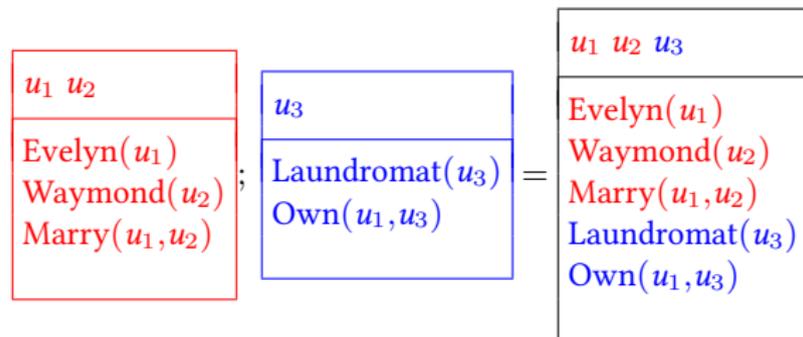
DRSs can be combined using **dynamic conjunction** (;).

(5) Evelyn marries Waymond. Evelyn owns a laundromat.



DRSs can handle **cross-sentential anaphora**.

(6) Evelyn<sub>1</sub> marries Waymond. She<sup>1</sup> owns a laundromat.





1 Recap

**2 Problem**

3 Compositional DRT

4 Practice



Classical DRT is not compositional!



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Q: Why is this a problem?



- 1 Forget about DRT and start over



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→ e.g. Dynamic Predicate Logic (Groenendijk and Stokhof 1991)
- 2 Make DRT compositional  
→ Compositional DRT (Muskens 1996)



1 Recap

2 Problem

**3** Compositional DRT

4 Practice



A sentence is a relation between an input state ( $i$ ) and an output state ( $o$ ).

$w$      $w$      $w$      $w$

$w$      $w$      $w$      $w$

$w$      $w$      $w$      $w$

$w$      $w$      $w$      $w$



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$w$     $w$     $w$     $w$

$w$     $w$     $w$     $w$

$w$     $w$     $w$     $w$

$w$     $w$     $w$     $w$

Evelyn  
is  
Asian. →

A sentence is a relation between an input state ( $i$ ) and an output state ( $o$ ).

w w w w

w w w w

w w w w

w w w w

Evelyn  
is  
Asian.  
→

w w w w

w w w w

w w w w

w w w w

(7) Evelyn is Asian.

$u_1$
Evelyn( $u_1$ ) Asian( $u_1$ )

(7) Evelyn is Asian.

$u_1$
Evelyn( $u_1$ ) Asian( $u_1$ )

$=_{abbr} \lambda i \lambda o. \dots$

(7) Evelyn is Asian.

$u_1$
Evelyn( $u_1$ ) Asian( $u_1$ )

$$=_{abbr} \lambda i \lambda o. i[u_1]o$$

where:

$$i[u_1]o =_{def} \forall u. u \neq u_1 \rightarrow \nu(i)(u) = \nu(o)(u)$$

and  $\nu(o)(u_1)$  maps dref  $u_1$  in state  $o$  to an individual (here Evelyn)

(7) Evelyn is Asian.

$u_1$
Evelyn( $u_1$ ) Asian( $u_1$ )

$$=_{abbr} \lambda i \lambda o. i[u_1]o \wedge \text{Evelyn}(\nu(o)(u_1)) \wedge \text{Asian}(\nu(o)(u_1))$$

where:

$$i[u_1]o =_{def} \forall u. u \neq u_1 \rightarrow \nu(i)(u) = \nu(o)(u)$$

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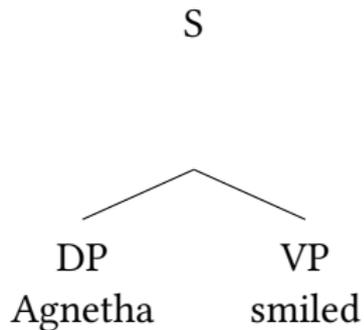
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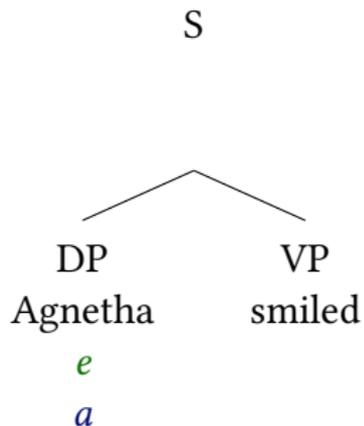
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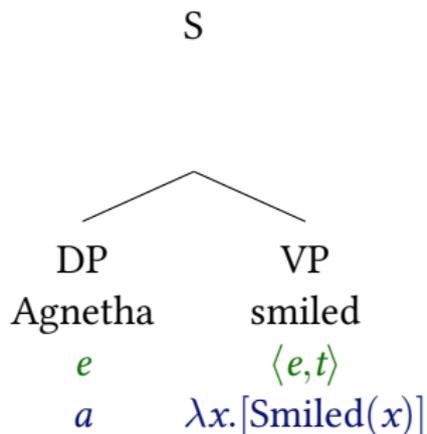
# Composition rule 1: Function Application



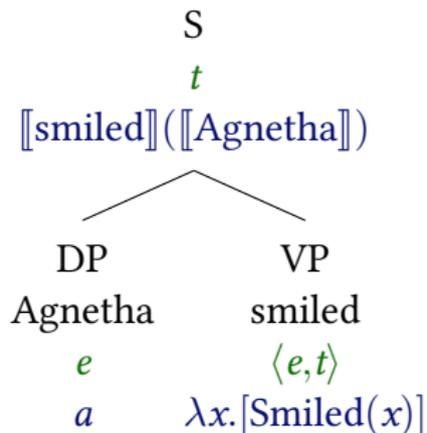
# Composition rule 1: Function Application



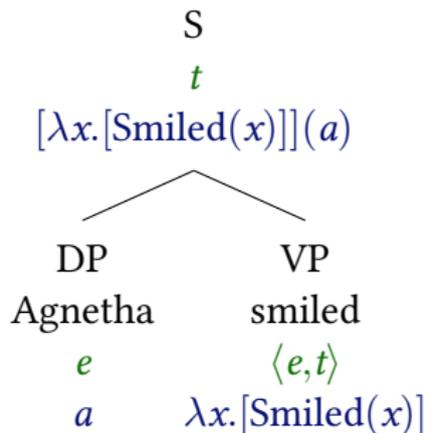
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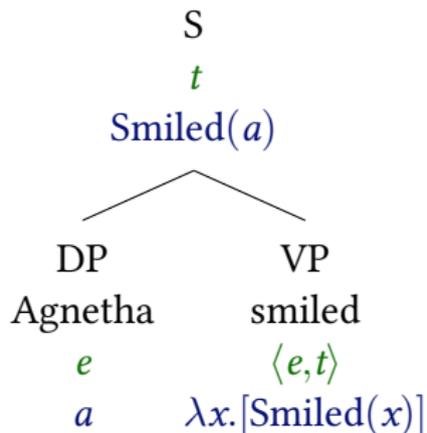
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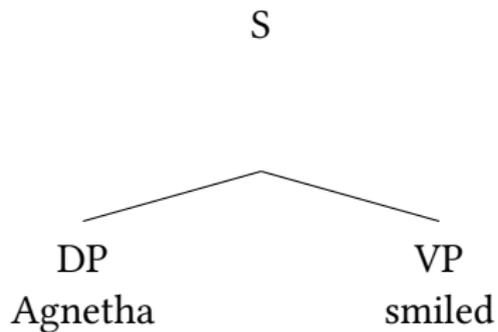
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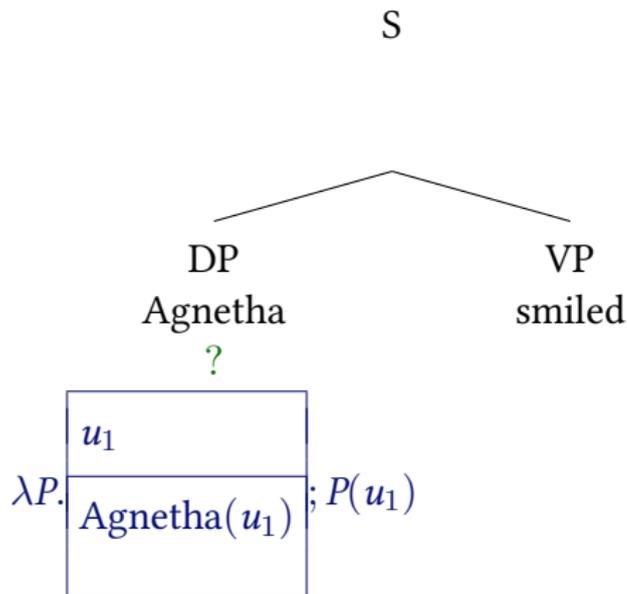


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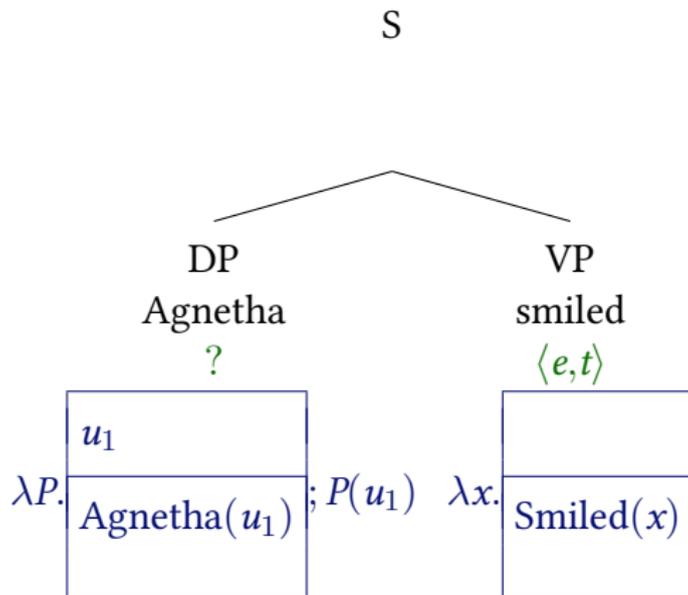




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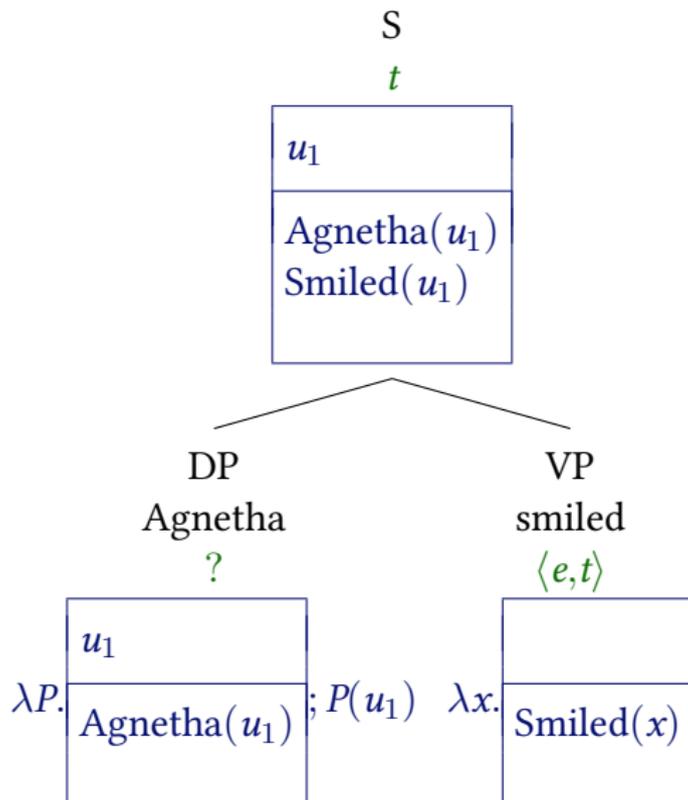








# Composition rule 1: Function Application



# Activity 1: Predicate nouns



Give the derivation of the following sentence:

(8) Agnetha is a singer.

- 1 Draw a syntactic tree.
- 2 Give the translations for the terminal nodes.  
(Assume that *is* and *a* have “no meaning”.)
- 3 Give the translations for the remaining nodes by applying Function Application.

## Activity 2: Predicate adjectives



Give the derivation of the following sentence:

(9) Björn is kind.

- 1 Draw a syntactic tree.
- 2 Give the translations for the terminal nodes.  
(Assume that *is* has “no meaning”.)
- 3 Give the translations for the remaining nodes by applying Function Application.

## Activity 3: Transitive verbs



Give the derivation of the following sentence:

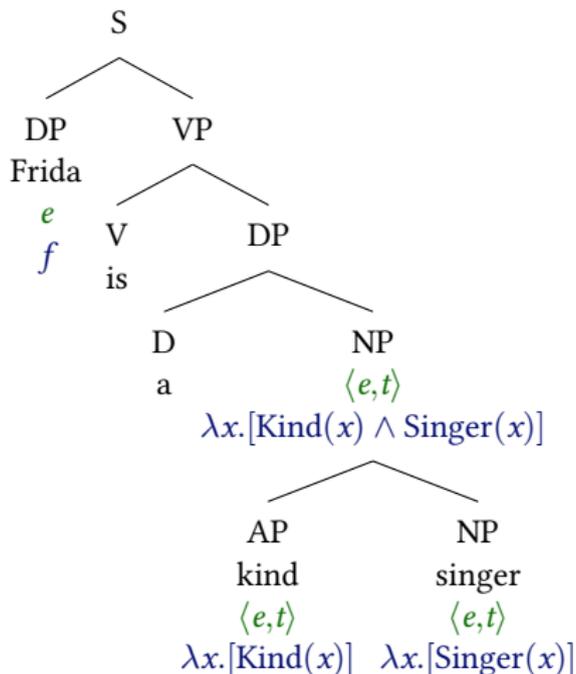
(10) Agnetha loved Björn.

- 1 Draw a syntactic tree.
- 2 Give the translations for the terminal nodes *Agnetha*, *loved* and *Björn*.
- 3 Give the translations for the remaining nodes by applying Function Application.

# Composition rule 2: Predicate Modification

Example: Attributive adjectives

Frida is a kind singer.

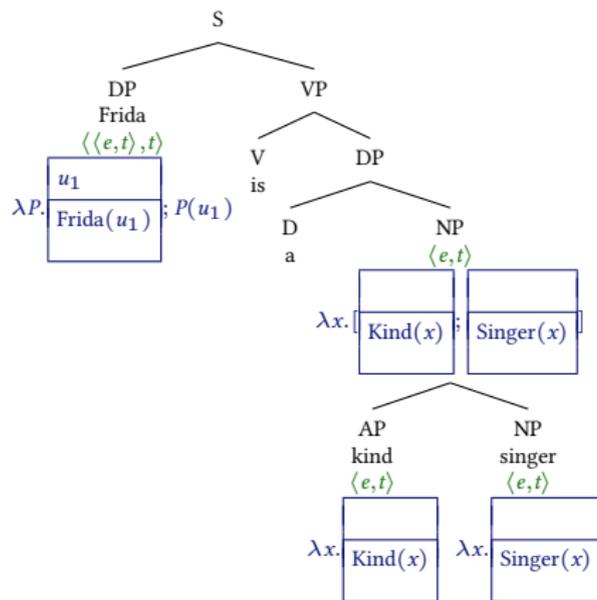




# Composition rule 2: Predicate Modification

Example: Attributive adjectives

Frida is a kind singer.



## Activity 4: Attributive adjectives (continued)



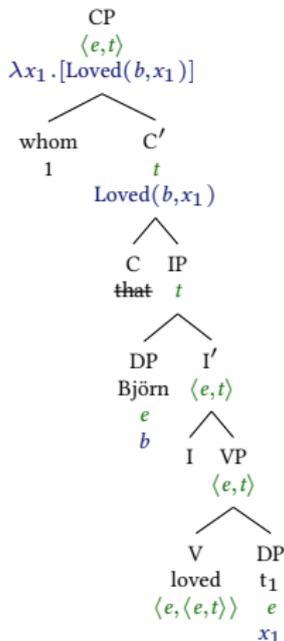
Give the derivation of the following sentence:

(11) Frida is a kind singer.

# Composition rule 3: Lambda Abstraction



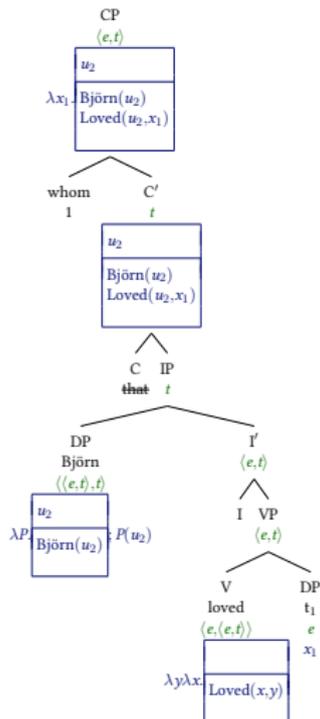
whom Björn loved





# Composition rule 3: Lambda Abstraction

whom Björn loved



## Activity 5: Lambda Abstraction



Give the derivation of the following sentences. Indicate the type of each node.

(12) Agnetha is a woman whom Bjorn loved.

(13) “Waterloo” is a song that Agnetha sang.



- Discourse representation theory can be made fully compositional.



Groenendijk, Jeroen, and Martin Stokhof. 1991. Dynamic Predicate Logic. *Linguistics and Philosophy* 14:39–100.

Muskens, Reinhard. 1996. Combining Montague Semantics and Discourse Representation. *Linguistics and Philosophy* 19:143–186.



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