

# Introduction to dynamic semantics

## Session 3: Plural discourse representation theory

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1 Recap

2 Plurals

3 Collective vs distributive readings

4 Cumulative readings

5 Plurals in DRT



Sentences introduce **discourse referents** and **conditions** on these drefs.



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Evelyn( $u_1$ ) Waymond( $u_2$ ) Marry( $u_1, u_2$ )

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# Recap

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The contribution of a sentence can be represented as a **discourse representation structure (DRS)**.

- (1) Evelyn<sup>1</sup> marries Waymond<sup>2</sup>.

$u_1$ $u_2$
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## Recap

The DRS of a sentence can be derived from its components.

## Recap

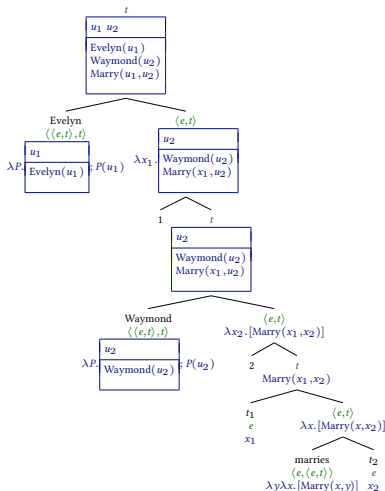
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# Recap

The DRS of a sentence can be derived from its components.

(2) Evelyn marries Waymond.



DRSs can be combined using **dynamic conjunction** (;).

(3) Evelyn marries Waymond. Evelyn owns a laundromat.

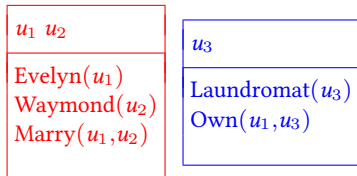
DRSs can be combined using **dynamic conjunction** (;).

(3) **Evelyn marries Waymond.** Evelyn owns a laundromat.

$u_1$ $u_2$
Evelyn( $u_1$ ) Waymond( $u_2$ ) Marry( $u_1, u_2$ )

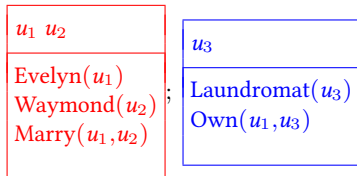
DRSs can be combined using **dynamic conjunction** (;).

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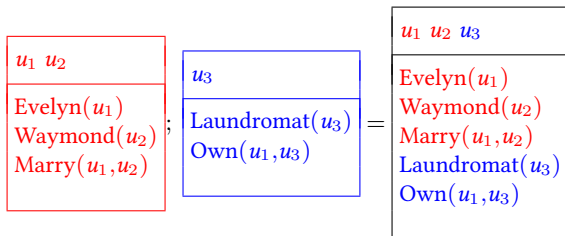
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How do we handle plurals?



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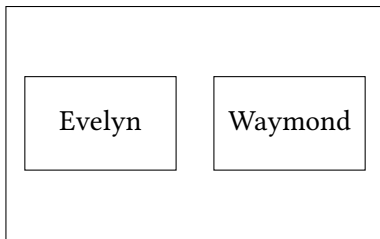
(4) Evelyn and Waymond smiled.

How do we handle plurals?

(4) Evelyn and Waymond smiled.

???
???

## Evelyn and Waymond



## Evelyn and Waymond



Evelyn

Waymond

## Evelyn and Waymond



Evelyn

Waymond





1 Recap

2 Plurals

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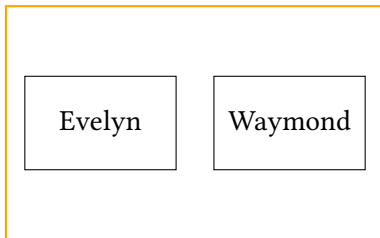
5 Plurals in DRT



(5) Evelyn and Waymond met.

(5) Evelyn and Waymond met.

Evelyn and Waymond

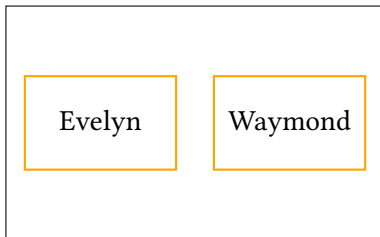




(6) Evelyn and Waymond smiled.

(6) Evelyn and Waymond smiled.

Evelyn and Waymond



# Activity 1: collective vs distributive readings



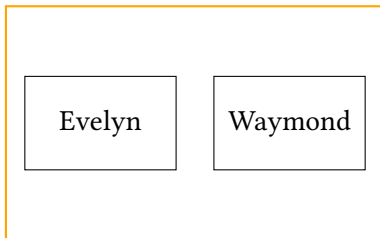
- 1 are numerous
- 2 are tall
- 3 ate a pizza
- 4 dispersed
- 5 gathered
- 6 laughed
- 7 read a book
- 8 scattered
- 9 watched a movie



(7) Evelyn and Waymond ate a pizza.

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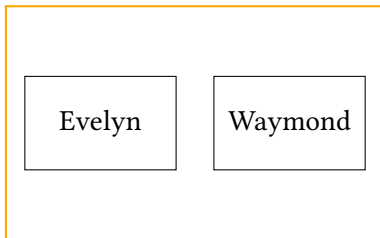
Evelyn and Waymond





(7) Evelyn and Waymond ate a pizza.

Evelyn and Waymond



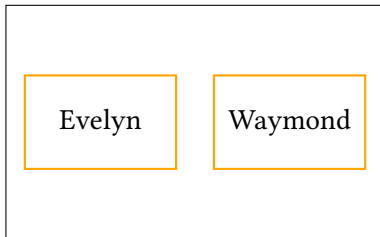
$Ate(E \oplus W, p)$



(8) Evelyn and Waymond ate a pizza.

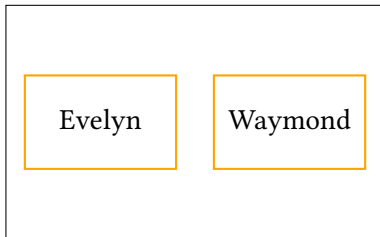
(8) Evelyn and Waymond ate a pizza.

Evelyn and Waymond



(8) Evelyn and Waymond ate a pizza.

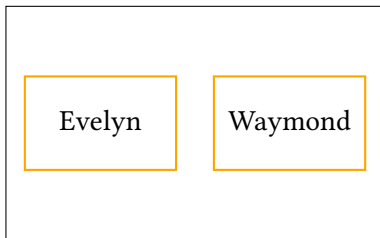
Evelyn and Waymond



$\approx \text{Ate}(\text{EACH}(E \oplus W), p)$

(8) Evelyn and Waymond ate a pizza.

Evelyn and Waymond



$\approx \text{Ate}(\text{EACH}(E \oplus W), p)$

Q: Is it the DP or the VP that “is plural”?



- DIST is an operator that applies to the predicate (in this case *ate*).



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- In general, we need to specify which argument we are distributing over.



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- In general, we need to specify which argument we are distributing over.
- On its distributive reading, the sentence *Evelyn and Waymond ate a pizza* roughly means:  
For each  $x$  that is a part of the sum of Evelyn and Waymond,  $x$  ate a pizza.





- From this point on, we will set distributive readings to one side.



- From this point on, we will set distributive readings to one side.
- Refer to the Appendix for more on intermediate (distributive) readings.



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**4 Cumulative readings**

5 Plurals in DRT

## Activity 2: Cumulative readings



What “readings” does the following sentence have?

(9) Evelyn, Waymond and Joy lifted three pianos.

(Ignore distributive readings.)



(10) Evelyn, Waymond and Joy lifted three pianos.

(10) Evelyn, Waymond and Joy lifted three pianos.

Collective reading:

	person	piano
$s$	$E \oplus W \oplus J$	$p_1 \oplus p_2 \oplus p_3$

# Cumulative readings

(10) Evelyn, Waymond and Joy lifted three pianos.

Collective reading:

	person	piano
$s$	$E \oplus W \oplus J$	$p_1 \oplus p_2 \oplus p_3$

Cumulative reading:

	person	piano
$s_1$	$E$	$p_1$
$s_2$	$W \oplus J$	$p_2 \oplus p_3$

# Cumulative reading: \* operator (Link 1983 *et seq.*)



Cumulative reading:

	person	piano
$s_1$	$E$	$p_1$
$s_2$	$W \oplus j$	$p_2 \oplus p_3$



## Cumulative reading: \* operator (Link 1983 *et seq.*)



Cumulative reading:

	person	piano
$s_1$	$E$	$p_1$
$s_2$	$W \oplus \mathcal{J}$	$p_2 \oplus p_3$

- \* is an operator that applies to the predicate (in this case \*\* applies to *lift*).

# Cumulative reading: \* operator (Link 1983 *et seq.*)



Cumulative reading:

	person	piano
$s_1$	$E$	$p_1$
$s_2$	$W \oplus J$	$p_2 \oplus p_3$

- \* is an operator that applies to the predicate (in this case \*\* applies to *lift*).
- Approximate meaning:
  - For each  $x$  that is a part of the sum of Evelyn, Waymond and Joy, there is a  $y$  that is a part of the pianos such that  $x$  lifted  $y$ .
  - For each  $y$  that is a part of the pianos, there is an  $x$  that is a part of the sum of Evelyn, Waymond and Joy such that  $x$  lifted  $y$ .



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- Plural (C)DRT treats DRSs as relations between plural information states, i.e., sets of information states.
- Conditions can be satisfied:
  - distributively within each information state or
  - collectively across all information states.

(11) Evelyn and Waymond smiled.

???
???



(12) Evelyn and Waymond smiled.



(12) Evelyn and Waymond smiled.

$u_1$
$E \oplus W(\cup u_1)$ Smiled( $u_1$ )

(12) Evelyn and Waymond smiled.

$u_1$
$E \oplus W(\cup u_1)$ Smiled( $u_1$ )

	$u_1$
$s_1$	$E$
$s_2$	$W$





(13) Evelyn and Waymond met.



(13) Evelyn and Waymond met.

$u_1$
$E \oplus W(\cup u_1)$ $\text{Met}(\cup u_1)$



(13) Evelyn and Waymond met.

$u_1$
$E \oplus W(\cup u_1)$ $\text{Met}(\cup u_1)$

	$u_1$
$s$	$E \oplus W$



(14) Evelyn, Waymond and Joy lifted three pianos.

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$u_1 \ u_2$
$E \oplus W \oplus \mathcal{J}(\cup u_1)$ 3-atoms( $\cup u_2$ ) Piano( $u_2$ ) Lifted( $u_1, u_2$ )

(15) Evelyn, Waymond and Joy lifted three pianos.

$u_1$ $u_2$
$E \oplus W \oplus \mathcal{J}(\cup u_1)$
$3\text{-atoms}(\cup u_2)$
$\text{Piano}(u_2)$
$\text{Lifted}(u_1, u_2)$

Collective “reading”:

	$u_1$	$u_2$
$s$	$E \oplus W \oplus \mathcal{J}$	$p_1 \oplus p_2 \oplus p_3$

Cumulative “reading”:

	$u_1$	$u_2$
$s_1$	$E$	$p_1$
$s_2$	$W \oplus \mathcal{J}$	$p_2 \oplus p_3$



(15) Evelyn, Waymond and Joy lifted three pianos.

$u_1$ $u_2$
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$\text{Piano}(u_2)$
$\text{Lifted}(u_1, u_2)$

Collective “reading”:

	$u_1$	$u_2$
$s$	$E \oplus W \oplus \mathcal{J}$	$p_1 \oplus p_2 \oplus p_3$

Cumulative “reading”:

	$u_1$	$u_2$
$s_1$	$E$	$p_1$
$s_2$	$W \oplus \mathcal{J}$	$p_2 \oplus p_3$

Q: Why is “reading” in quotes?

(15) Evelyn, Waymond and Joy lifted three pianos.

$u_1$ $u_2$
$E \oplus W \oplus \mathcal{J}(\cup u_1)$
$3\text{-atoms}(\cup u_2)$
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$\text{Lifted}(u_1, u_2)$

Collective “reading”:

	$u_1$	$u_2$
$s$	$E \oplus W \oplus \mathcal{J}$	$p_1 \oplus p_2 \oplus p_3$

Cumulative “reading”:

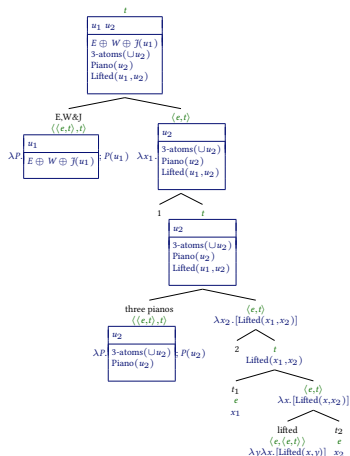
	$u_1$	$u_2$
$s_1$	$E$	$p_1$
$s_2$	$W \oplus \mathcal{J}$	$p_2 \oplus p_3$

Q: Why is “reading” in quotes?

Q: Is this simpler than an operator-based approach?



(16) Evelyn, Waymond and Joy lifted three pianos.





- Sentences with plurals have different “readings”: e.g. collective, distributive, cumulative...



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- Plural (C)DRT treats DRSs as relations between plural information states.

## Further reading

### Overviews:

- 1 Nouwen (2016)
- 2 Haug and Dalrymple (2020)

### Technical details of plural (C)DRT

- 1 van den Berg (1996)
- 2 Brasoveanu (2007)

## Activity: Intermediate readings

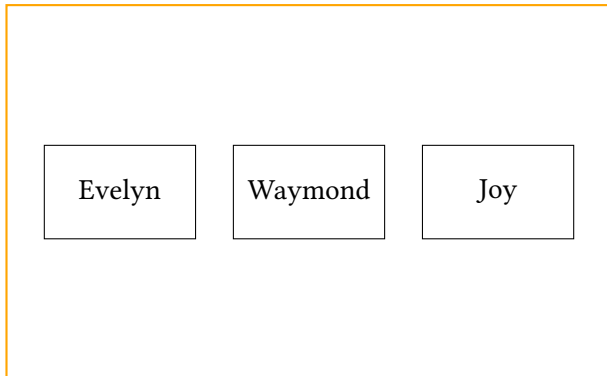


What “readings” does the following sentence have?

(17) Evelyn, Waymond and Joy ate a pizza.

(18) Evelyn, Waymond and Joy ate a pizza.

Evelyn, Waymond and Joy



(19) Evelyn, Waymond and Joy ate a pizza.

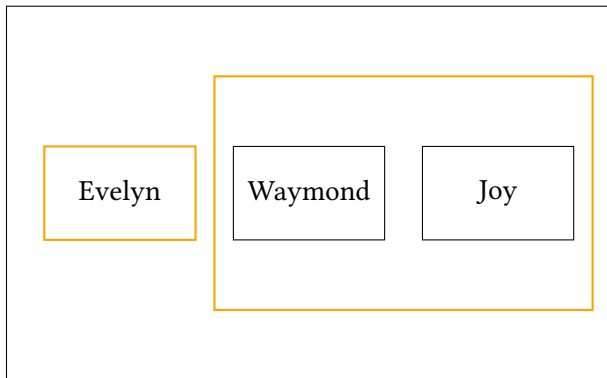
Evelyn, Waymond and Joy



# Intermediate distributive reading

(20) Evelyn, Waymond and Joy ate a pizza.

Evelyn, Waymond and Joy

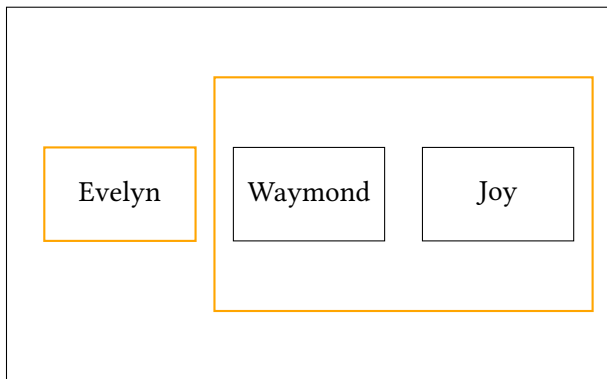




# Intermediate distributive reading

(20) Evelyn, Waymond and Joy ate a pizza.

Evelyn, Waymond and Joy



Q: Do you get this reading?



- Brasoveanu, Adrian. 2007. Structured nominal and modal reference. Doctoral dissertation, Rutgers University.
- Haug, Dag Trygve Truslew, and Mary Dalrymple. 2020. Reciprocity: Anaphora, scope, and quantification. *Semantics and Pragmatics* 13:1–62.
- Link, Godehard. 1983. The logical analysis of plurals and mass terms: A lattice-theoretical approach. In *Meaning, Use, and Interpretation of Language*, ed. Rainer Bäuerle, Christoph Schwarze, and Arnim Von Stechow, 302–323. Berlin: De Gruyter.
- Nouwen, Rick. 2016. Plurality. In *The Cambridge Handbook of Formal Semantics*, ed. Maria Aloni and Paul Dekker, 267–284. Cambridge: Cambridge University Press.
- van den Berg, Martin. 1996. Some aspects of the internal structure of discourse: The dynamics of nominal anaphora. Doctoral dissertation, University of Amsterdam.